Issues Associated with the Visualization and Significance of Bus Phase Angles for the Eastern Interconnect



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# A Motivation: 8/14/03 Angle Separation



Slide source: Robert Cummings (NERC) November 29, 2007 PMU Overview and Update Presentation

Slide at left indicates that during the 8/14/03 event there was a significant angle separation between Cleveland and Western MI. But it also raises some interesting research questions

## Bus Angle Visualization: 8/14/03 Day Ahead Model



## Bus Angle Visualization: 8/14/03 16:05 EDT (Reconstructed)



## What Does A Bus Angle Indicate?

- Straightforward (if we allow for a dc power flow approximation):  $\mathbf{\theta} = \mathbf{B}^{-1}\mathbf{P}$ 
  - -Incremental variations similar for full ac case
- The equation indicates that the angle at a particular bus is the vector product of a row of the inverse of the B matrix with the net power injection vector **P**.
- While the B matrix is sparse, its inverse is not.
- Angles are given with respect to a system reference, Brown's Ferry here (18137)



#### Example: In NERC 2008 Summer Case Angle at <sup>6</sup> 36406 (Wempleton 345 in Northern IL) is -25.2°





## Angle Difference Between Wempleton and Burnham 345 kV



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**PSERC** 

#### **Zoomed View of Midwest**



#### Variation in Angle across Northern Illinois (One Month SCOPF Simulated Data)



Average = 9.6 degrees, standard deviation =  $3.8 \text{ degrees}_{PSERC}$ 

#### Variation in Angle from W. MI to Central OH (One Month SCOPF Simulated Data)



Average = 10.7 degrees, standard deviation =  $3.1 \text{ degree}_{\text{SERC}}$ 

## **Summary and Future Work**

- In the Eastern Interconnect the significance of individual bus angles or bus angle differences across different regions is not fully understood.
- We would like to suggest future work in which the theoretical and practical issues associated with the interpretation of phase angle differences are studied.
- Useful input data would be a set of state estimator cases to give actual operating conditions coupled with associated PMU measurements.
- Results would (hopefully) be interpretations and visualizations of this data

