



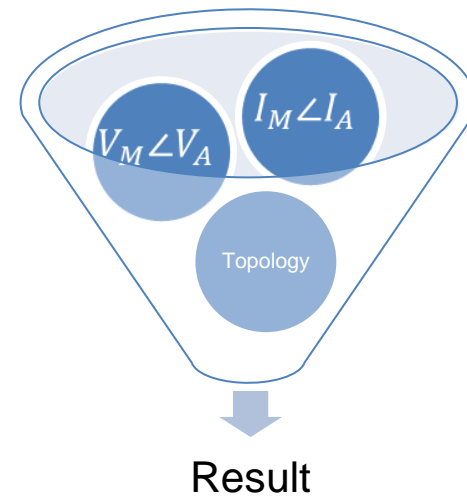
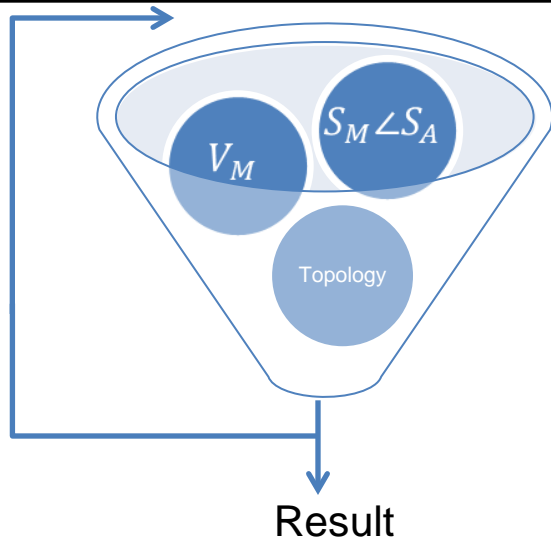
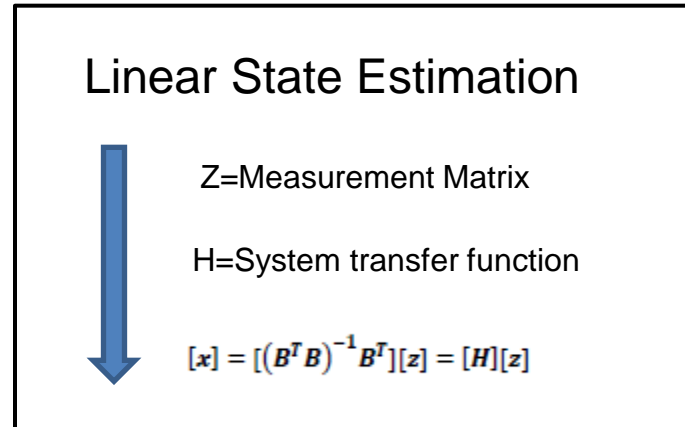
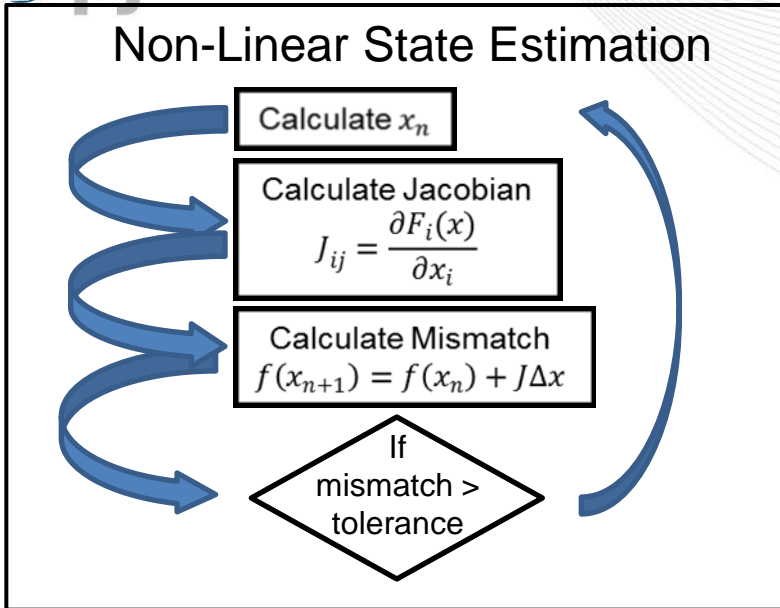
Synchrophasor Data Analytics

Linear State Estimation Using Phasor Measurement Unit Data

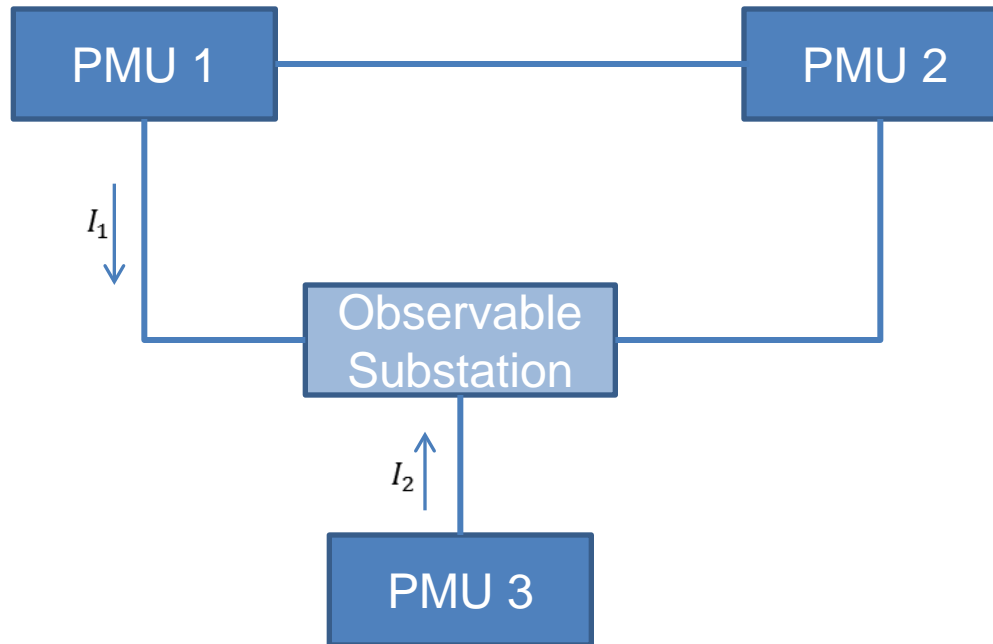
Shaun Murphy, ARC Engineer

March 25, 2015

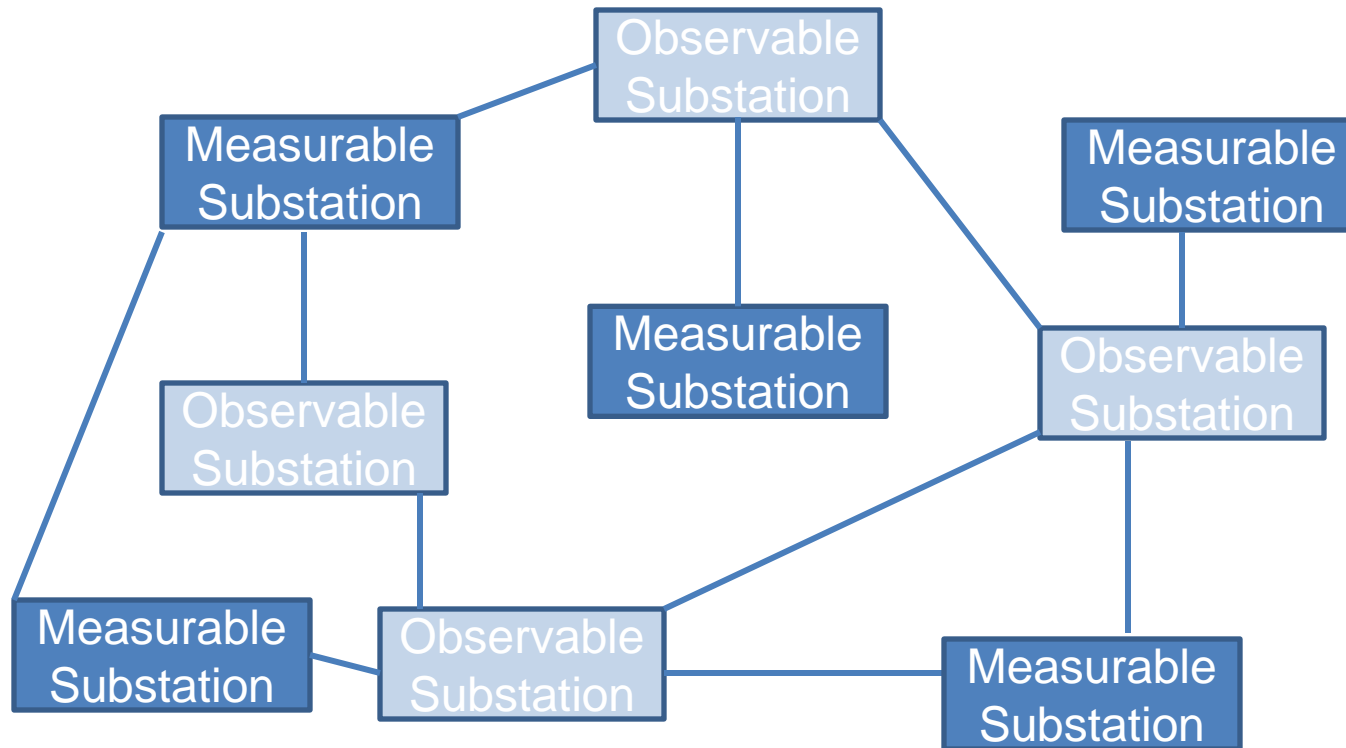
- What is a Linear State Estimator (LSE)?
- Observability
- Leveraging Redundancy: PJM's Observable and Measureable Substations
- PJM's Implementation of the Linear State Estimator Algorithm
- Lessons Learned & Engaging with our Transmission Owners
- Plans for the Future



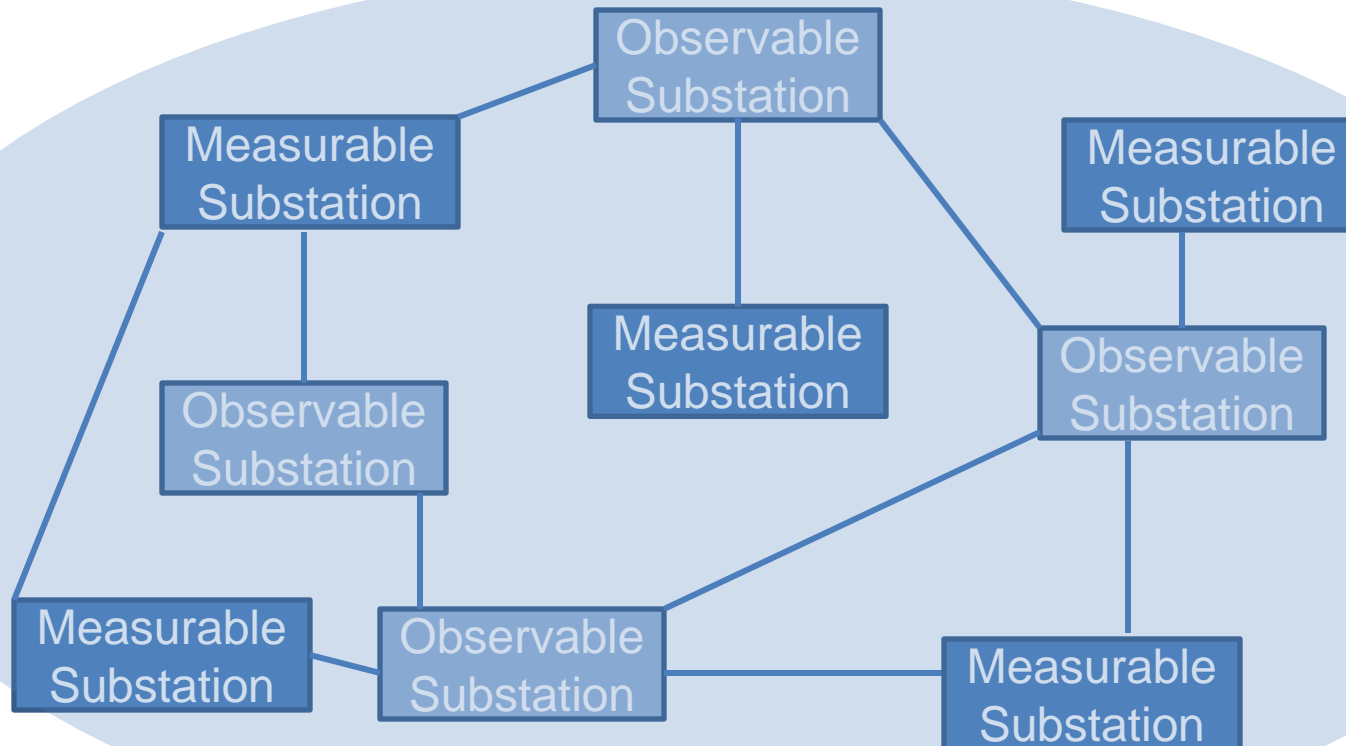
- A Linear State Estimator can be used to infer PMU equivalents, where substations without PMU measurements can still be monitored



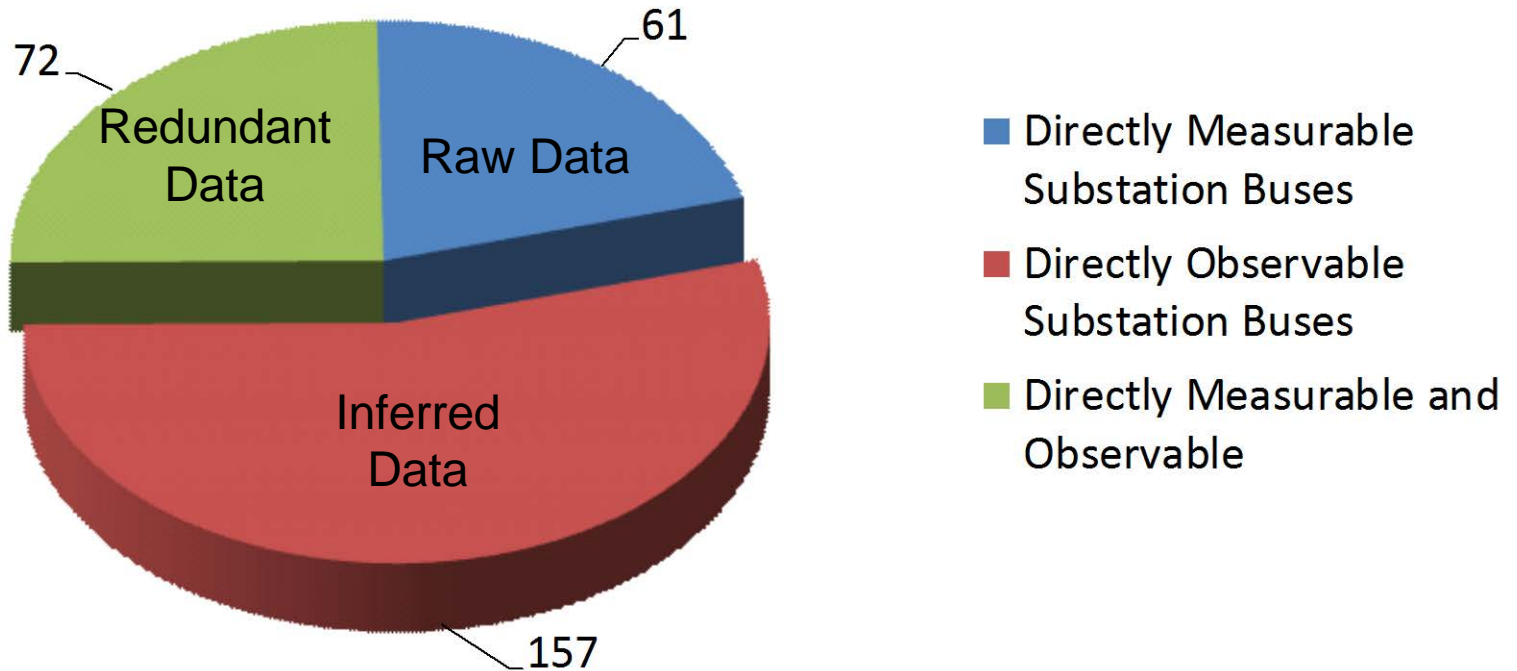
- A Linear State Estimator fills-in the picture of our grid.
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Leveraging Redundancy: PJM's Observable and Measureable Substations





- PMU data retrieved from RTDMS via SQL Query
- Source code written in Statistical Analytic Software (SAS)
- Scheduled job executed every 15 minutes for 30 consecutive data frames.
- Results outputted to PI Historian



- C37 Status Word
- Voltage Magnitude between 0.7 and 1.3 Per Unit
- **Average bus voltage between 0.7 and 1.3 Per Unit**
- Current Magnitude less than 50 Per Unit
- Other Special Errors



Inputs:

- PMU data passing the Plausibility Checks
- Breaker Statuses
- Impedance Data

Output:

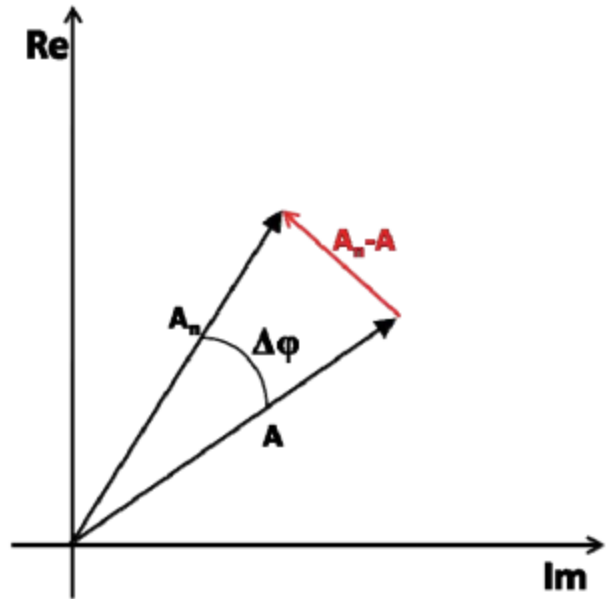
- System state of all observable substations

$$[x] = [(B^T B)^{-1} B^T][z] = [H][z]$$



1. Compute all measurement signals based on the result of the LSE algorithm.
2. Compute Total Vector Error using raw PMU data and the computed measurement value.

$$TVE = \sqrt{\frac{(A_r(n) - A_r)^2 + (A_i(n) - A_i)^2}{A_r^2 + A_i^2}}$$





Lessons Learned & Engaging with Our Transmission Owners

- Individual configuration errors identified and corrected.
- Signal dropouts identified more quickly.
- Handling of outages to PMU signals.
- Plausibility Check performance can be trended and shared with our Transmission Owners.
- Eventually, we will share TVE Calculations based on results from the Linear State Estimator.

Short-Term Issues

- Intermittent Signal Drop-outs
- Alignment of LSE results with SE phase angles

Longer-Term Issues

- Sustained Signal Drop-outs
- Permanent corrections to PMU data stream issues
- Management of calculated data

Opportunities

- Improvement to Data Quality – Additional Reporting to our Transmission Owners
- New insights to the electric grid

